

Quantum Application Survey: Progress in Analog Quantum Computing

Xiaodi Wu

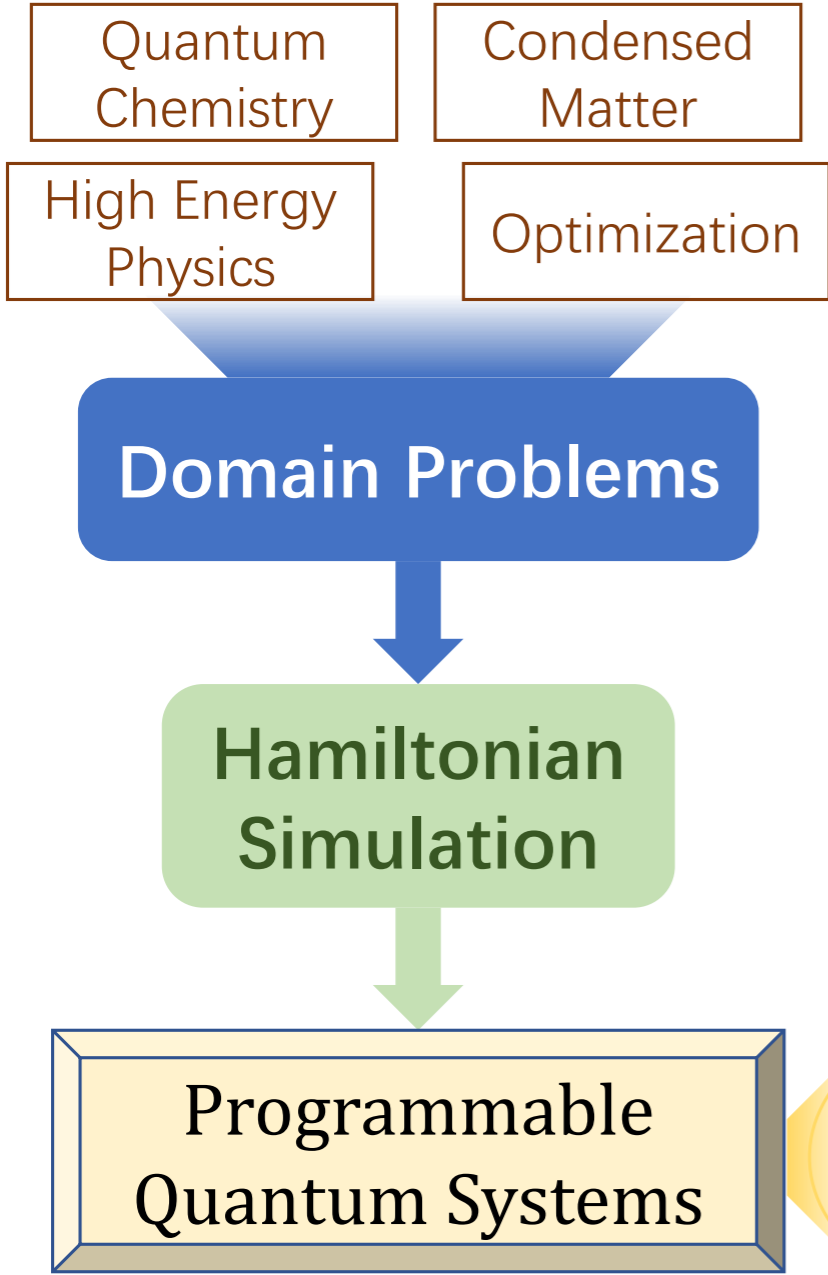
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Physics-simulation-based Quantum Applications



>20 papers published since 2020 in Physics Review & Nature series

Article | Published: 30 November 2022
Traversable wormhole dynamics on a quantum processor

Daniel Jaffe | Article | Published: 07 July 2021
Davis, Nikolai | **Quantum simulation of 2D antiferromagnets with hundreds of Rydberg atoms**
Nature 612

Pascal Scholl | Article | Published: 18 November 2020
Daniel Barre | **Observation of gauge invariance in a 71-site Bose-Hubbard quantum simulator**
Thomas C. L. | *Nature* 595
Bing Yang, Hui Sun, Robert Ott, Han-Yi Wang, Torsten V. Zache, Jad C. Halimeh, Zhen-Sheng Yuan, Philipp Hauke & Jian-Wei Pan
Nature 587, 392–396 (2020) | [Cite this article](#)

Editors' Suggestion
Trailhead for quantum simulation of SU(3) Yang-Mills lattice gauge theory in the local multiplet basis
Anthony Ciavarella | *Phys. Rev. D* 103

Quantum simulation of nuclear inelastic scattering
Weijie Du, James P. Gaebler | *Phys. Rev. A* 104

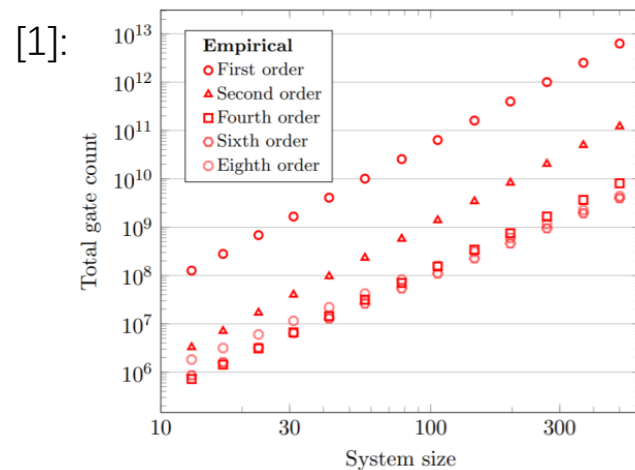
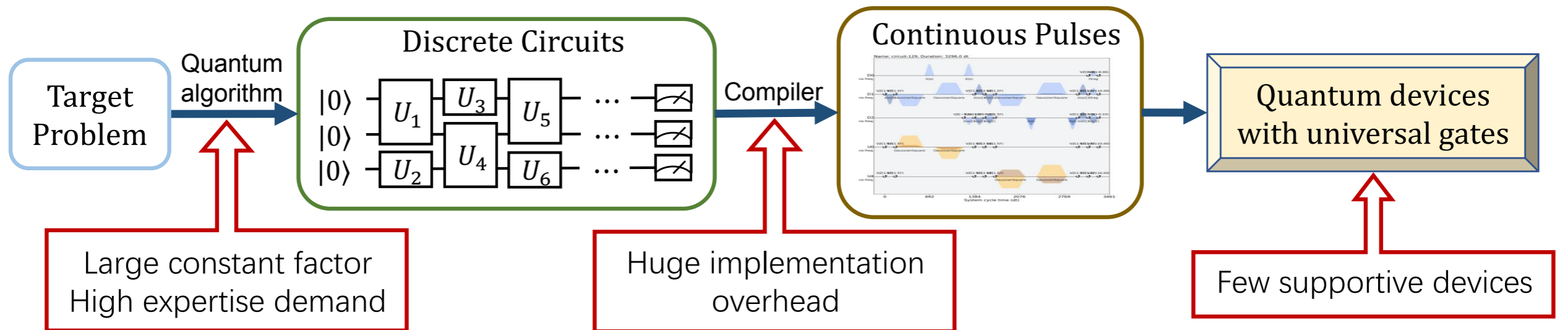
Simulating the dynamics of braiding of Majorana zero modes using an IBM quantum computer
John P. T. Stenger, Nicholas T. Bronn, Daniel J. Egger, and David Pekker
Phys. Rev. Research 3, 033171 – Published 20 August 2021



- A major application of quantum computing with early feasibility
- Amenable to both circuit-model and Hamiltonian-model implementation
- Recent pulse-level control of quantum devices enables investigation of both

Circuit-based Digital Implementation is Expensive

Digital Quantum Computing Paradigm



On IBM devices:
 $10 \cdot T_{\text{CNOT}} \approx T_1 \approx T_2$
 $T_{RXX(\theta)} \approx 2 \cdot T_{\text{CNOT}}$

Available:
 Superconducting
 Ion Trap

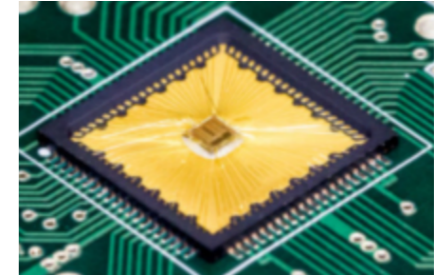
[1]: Childs et al., Toward the first quantum simulation with quantum speedup, PNAS, 2018.

- Circuit-model is a well-recognized theoretical model/interface between quantum applications and hardware, w/ merits in its mathematical elegance.
- Overheads w/ circuit abstraction. Resource-Efficient Quantum Computing by Breaking Abstractions [IEEE]
- Mismatch in quantum & classical hardware specs: clock rate, hardware acceleration
- Asymptotic theoretical speedup (circuit) \neq > speedup in practice [CACM, May 2023; q. IPM]

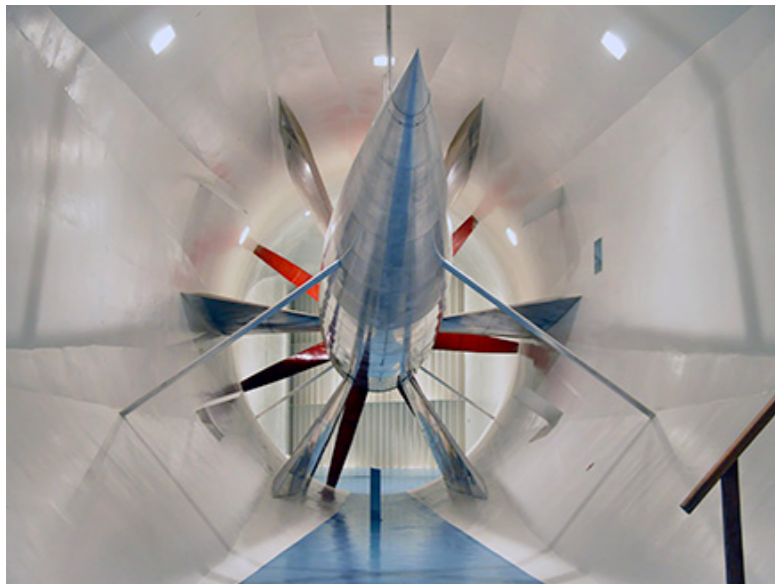
Hamiltonian-based Analog Machines

Analog computing predates digital computing, and revives recently due to challenges in scaling up digital computing (e.g. Moore's law).

- *Energy Efficiency — low overhead*
- *Domain applications like analog AI chip*



HCDCv2 Analog Devices
(Columbia University)



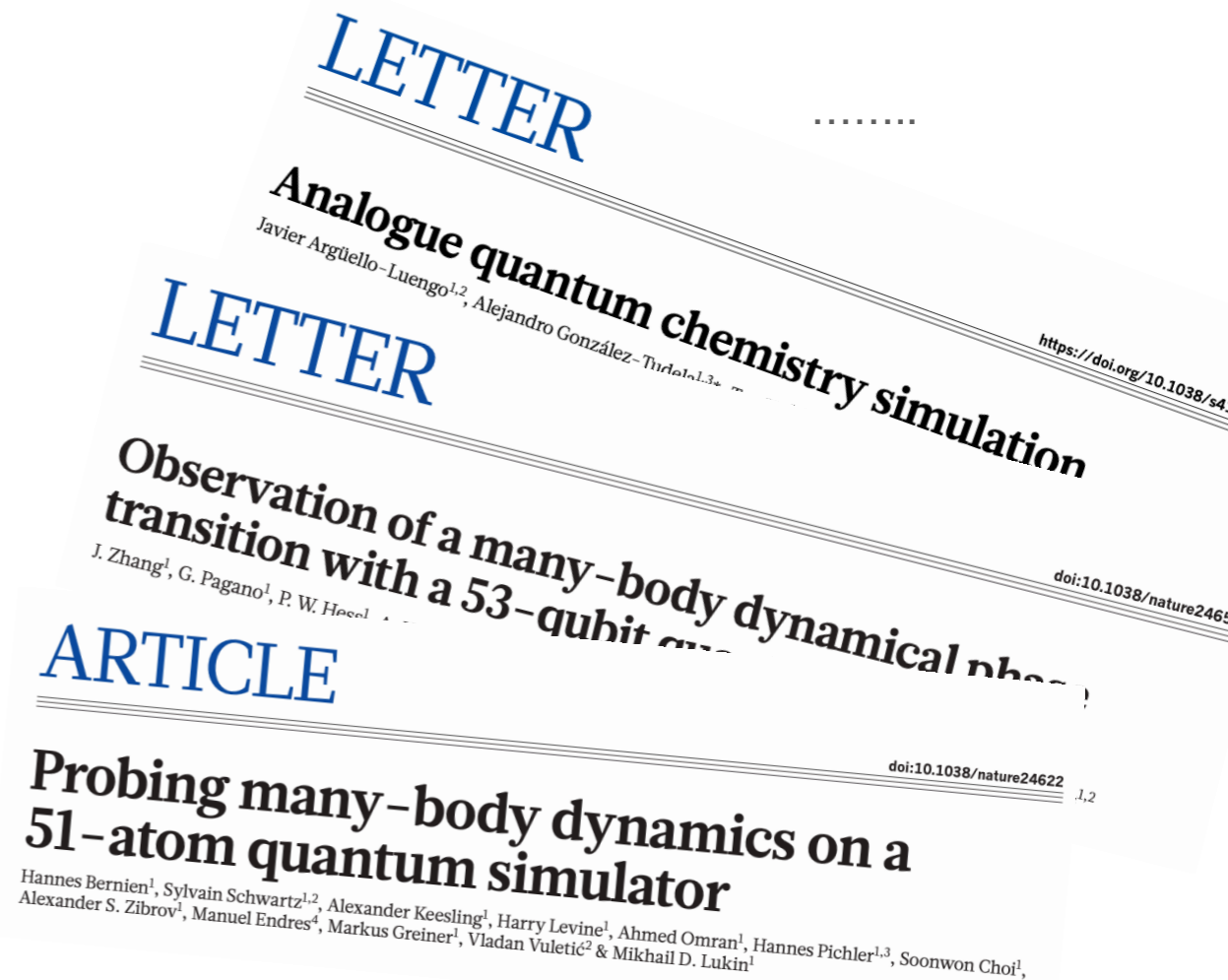
Wind Tunnels & Various Testbeds remain the standard solutions in practice for many domain applications.

Analog Quantum Simulators are not unfamiliar either.

The Analog Milestone for QC:

Understand unknown physics w/ help of analog/special-purpose quantum machines!

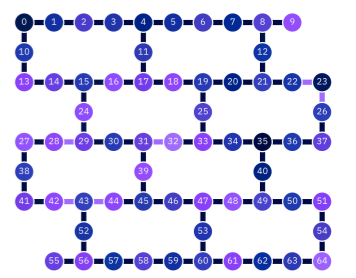
We believe **analog thinking & tool-chain** will be critical to achieve this milestone!



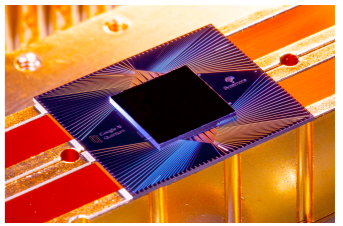
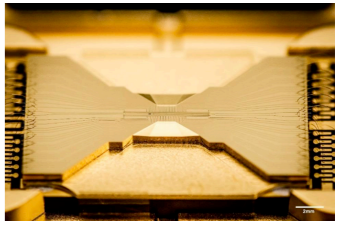
Conceptual Differences between circuit and Hamiltonian models

DIGITAL

ANALOG



Quantum Hardware



Parameterized Quantum Circuits

Variational Q. Methods

Circuits to describe everything

Algorithm & Complexity

Differentiable Quantum Physics

Variational Q. Methods

Hamiltonian Simulation

Algorithm & Complexity

problems from scientific computing, operation research, machine learning

Gate/Circuit-based Abstraction

Hamiltonian-based Abstraction



PL to model gate/circuits

Programming Languages

Qubit/Gate as basic primitives

Hardware Design&Control

PL to model Hamiltonian Evolution

Programming Languages

Pulse-level Control as basic primitives

Hardware Design&Control

Pulse-level control enables the investigation of the latter

Examples of Hamiltonian-based Demonstration

- Physical phenomena: quantum scar, phase transition, spin liquid, or so
- Neutral atoms (QuERA, Pasqal), Trapped Ions, Superconducting (IBM, Rigetti)
- Leverage native programmability of quantum devices, but w/ more complicated error models, lacks a fault-tolerant theory and a nontrivial use of native Hamiltonian (for now)

LETTER

<https://doi.org/10.1038/s41586-019-1614-4>

Analogue quantum chemistry simulation

Javier Argüello-Luengo^{1,2}, Alejandro González-Tudela^{1,3*}, Tao Shi^{1,4}, Peter Zoller^{1,5} & J. Ignacio Cirac^{1,6*}

LETTER

doi:10.1038/nature24654

Observation of a many-body dynamical phase transition with a 53-qubit quantum simulator

J. Zhang

ARTICLE

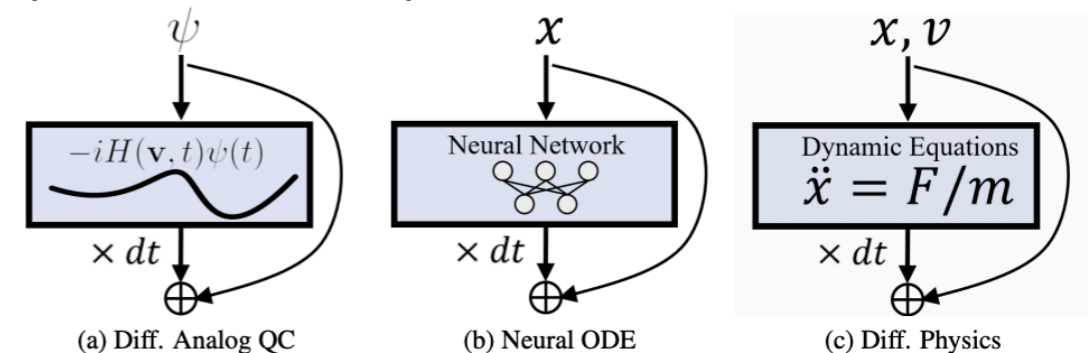
doi:10.1038/nature24622

Probing many-body dynamics on a 51-atom quantum simulator

Hannes Bernien¹, Sylvain Schwartz^{1,2}, Alexander Keesling¹, Harry Levine¹, Ahmed Omran¹, Hannes Pichler^{1,3}, Soonwon Choi¹, Alexander S. Zibrov¹, Manuel Endres⁴, Markus Greiner¹, Vladan Vuletić² & Mikhail D. Lukin¹

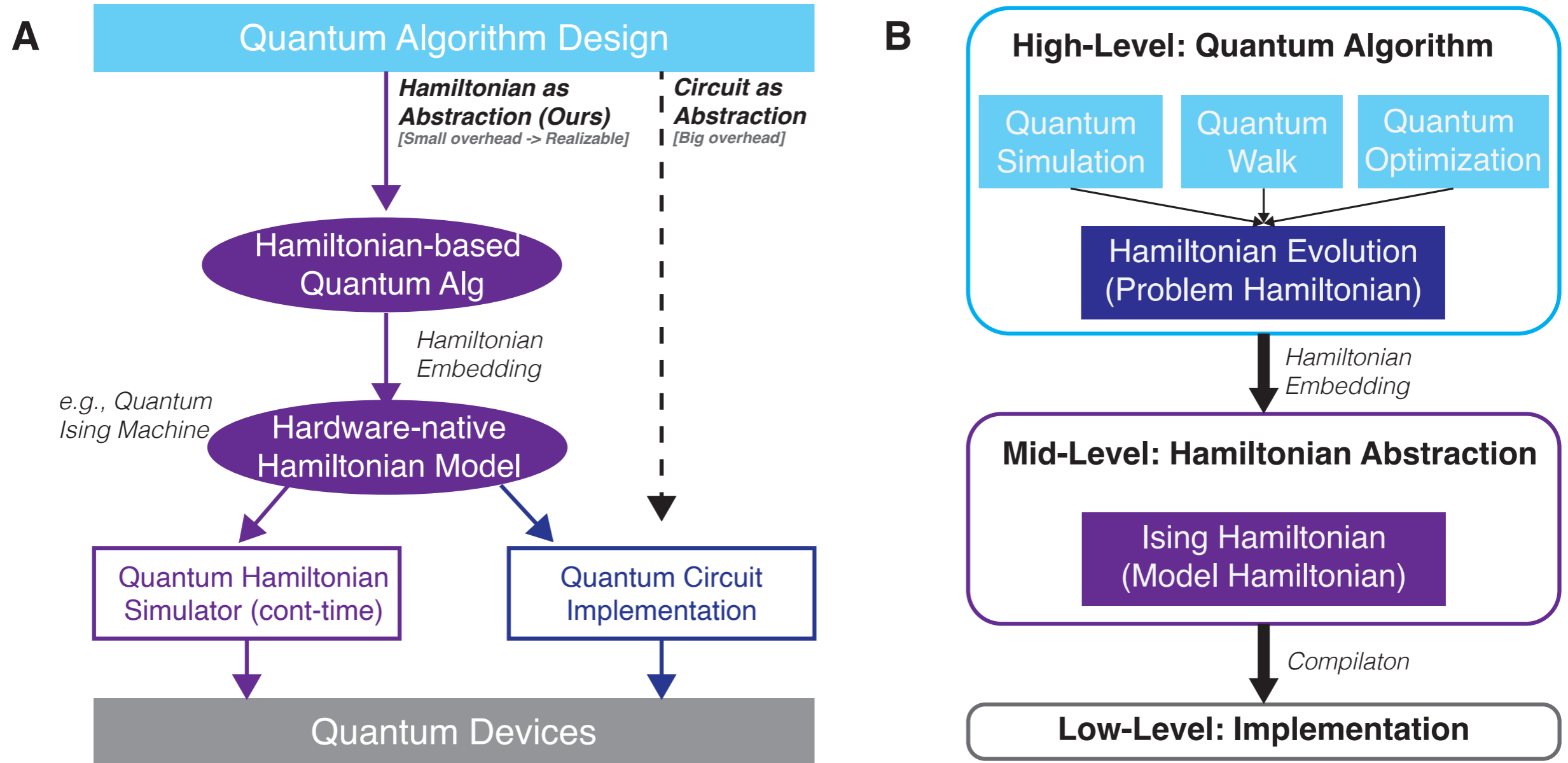
Simulation -> Differentiable Simulation / variational methods

- Leveraging pulse-ansatz for variational methods: 2008.04302, 2202.08908, 2208.01215, 2211.02584, 2211.02748, 2212.12911, 2304.09253, and so on....



- We developed an auto-differentiation training method for differentiable quantum physics (NeurIPS 2022), demonstrate orders of magnitude advantage on simulators.

Hamiltonian-oriented Algorithm Design: beyond naive cases



- Hamiltonian-oriented design: both (1) **new quantum algorithms** and (2) **more efficient implementation** of existing quantum algorithms
- Apply to both *near-term* and *long-term* quantum devices
- Key new technique in implementation is the **Hamiltonian embedding** scheme

Hamiltonian-oriented Algorithm Design: Examples

Continuous Optimization

Quantum PDE Solvers

Particle in real space & Dirac equation

Quantum Walk & Spatial Search

New Quantum Algorithm

Quantum Hamiltonian Descent

derived from the *path integral* of continuous-time classical gradient flow

Superior Performance in TTS (Time-To-Solution) than *quantum adiabatic* and *five classical SOTA algs* on **75-dim** quadratic programming instances

Quantum PDE Solver for

First-order hyperbolic equations (e.g, Hamilton-Jacobi, Heat, Liouville's)

Via embedding classical dynamics into Schrödinger equation

No new quantum algorithm

New Implementation: Hamiltonian Embedding

Hamming Encoding Quantum Ising Machine

Unary encoding + Anti-Ferromagnetic (AF) Quantum Ising Machine

Anti-Ferromagnetic (AF) + One-shot Encoding Quantum Ising Machine

Platforms

Using D-Wave as an analog quantum simulator

Neutral Atoms

Neutral Atoms/Trapped Ions

Hamiltonian-oriented Algorithm Design: Examples

Continuous Optimization

New Quantum Algorithm

Quantum **H**amiltonian **D**escent
 derived from the *path integral* of continuous-time classical gradient flow

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New Implementation: Hamiltonian Embedding

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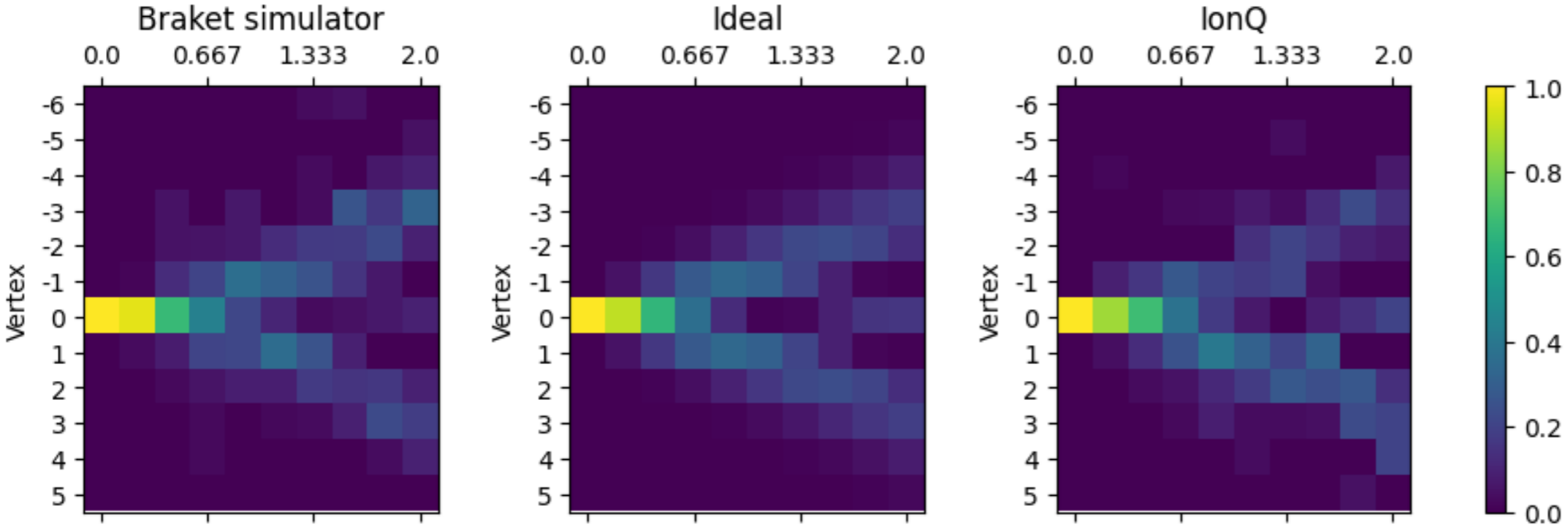
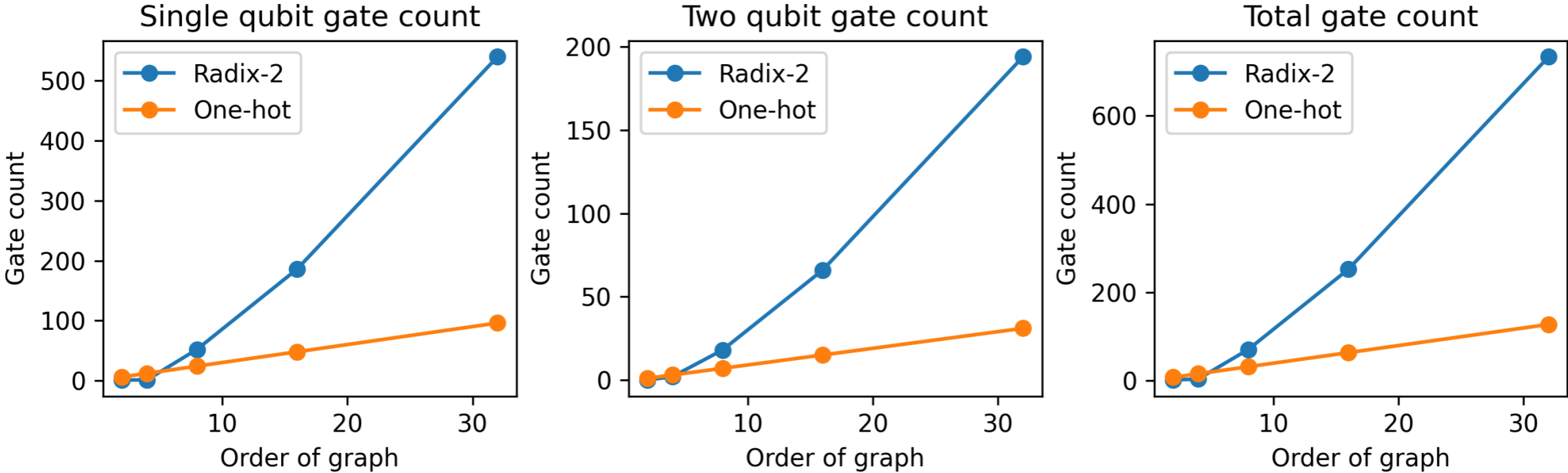


QHD Website

Quantum PDE Solvers	Particle in real space & Dirac equation	Quantum Walk & Spatial Search
Quantum PDE Solver for First-order hyperbolic equations (e.g, Hamilton-Jacobi, Heat, Liouville's)	No new quantum algorithm	
Via embedding classical dynamics into Schrödinger equation		Manuscript Under-Preparation
Unary encoding + Anti-Ferromagnetic (AF) Quantum Ising Machine	Anti-Ferromagnetic (AF) + One-shot Encoding Quantum Ising Machine	
Neutral Atoms	Neutral Atoms/Trapped Ions	

1-D quantum walk example: early view on IonQ Aria

IonQ resource estimate for quantum walk

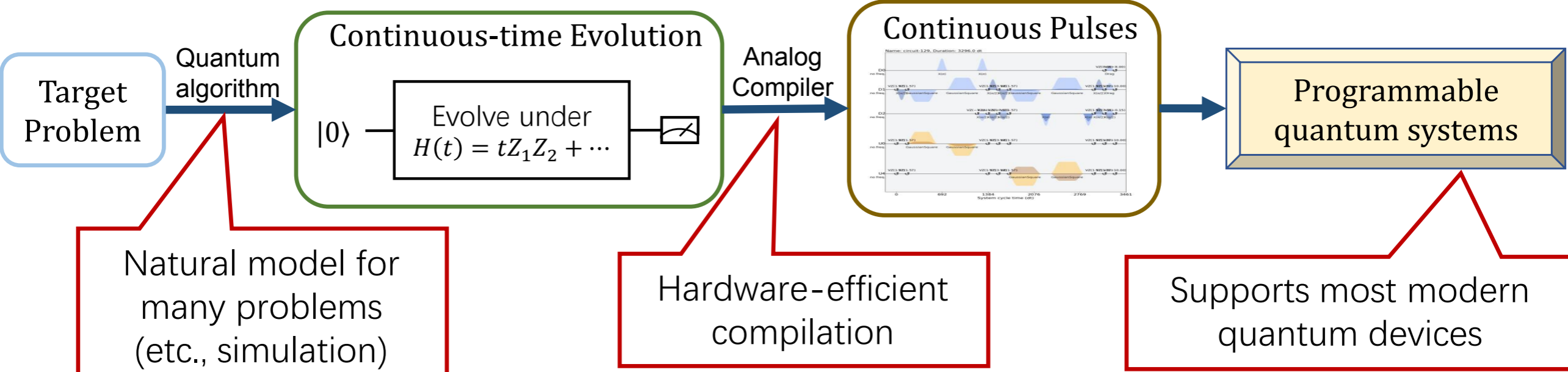


Example:
 12-vertices 1-D quantum walk
 Via one-shot encoding
 Accessed on 05-17-23
 33 USD on Braket

Infrastructure for Hamiltonian-oriented Programming

Ready for modern quantum devices!

Analog (Hamiltonian-oriented) Quantum Computing Paradigm



ABSTRACTION & SOFTWARE?



SIMUQ

SIMUlation language for **Q**uantum



GitHub repo:

<https://github.com/PicksPeng/SimuQ>

Enhance your capability of harnessing the power of quantum devices

arXiv: 2303.02775

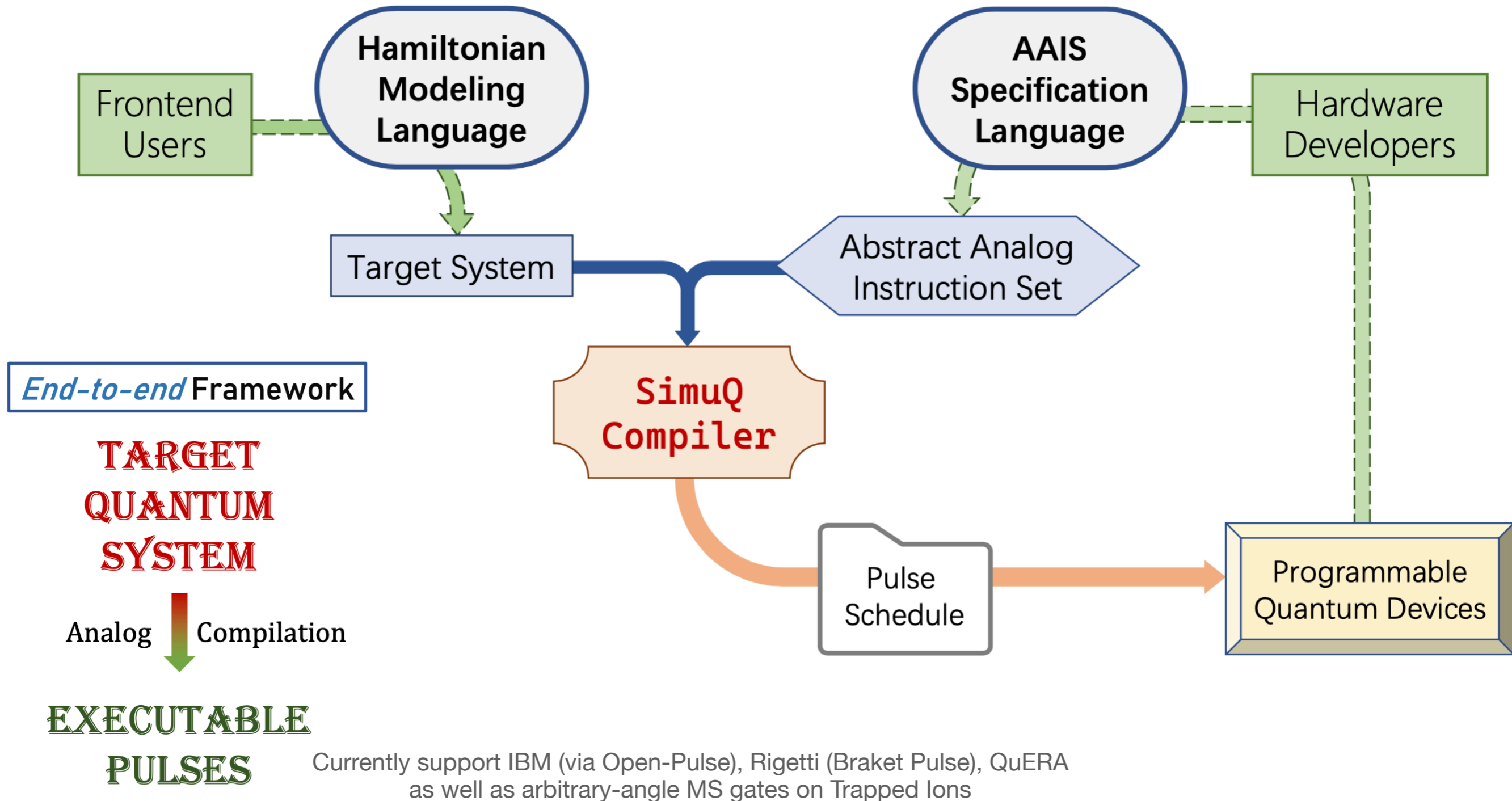


Project website:

<https://pickspeng.github.io/SimuQ/>

SimuQ Framework

All our Hamiltonian-oriented applications are now coded w/ SimuQ !!!



GitHub repo:

<https://github.com/PicksPeng/SimuQ>

Enhance your capability of harnessing the power of quantum devices

[arXiv: 2303.02775](https://arxiv.org/abs/2303.02775)



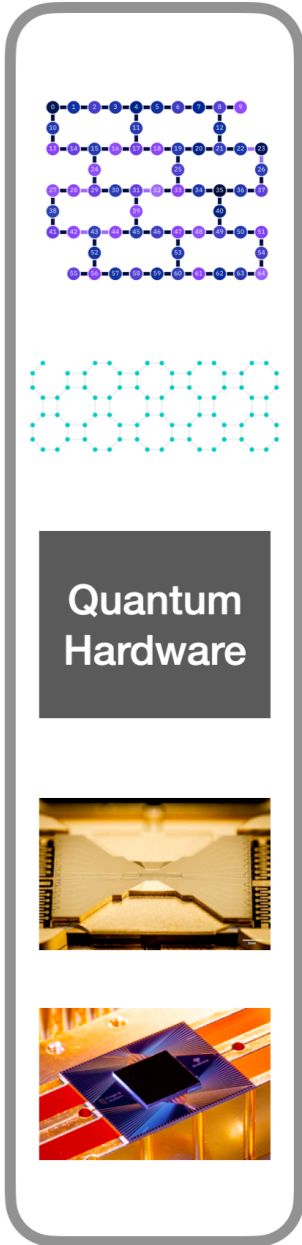
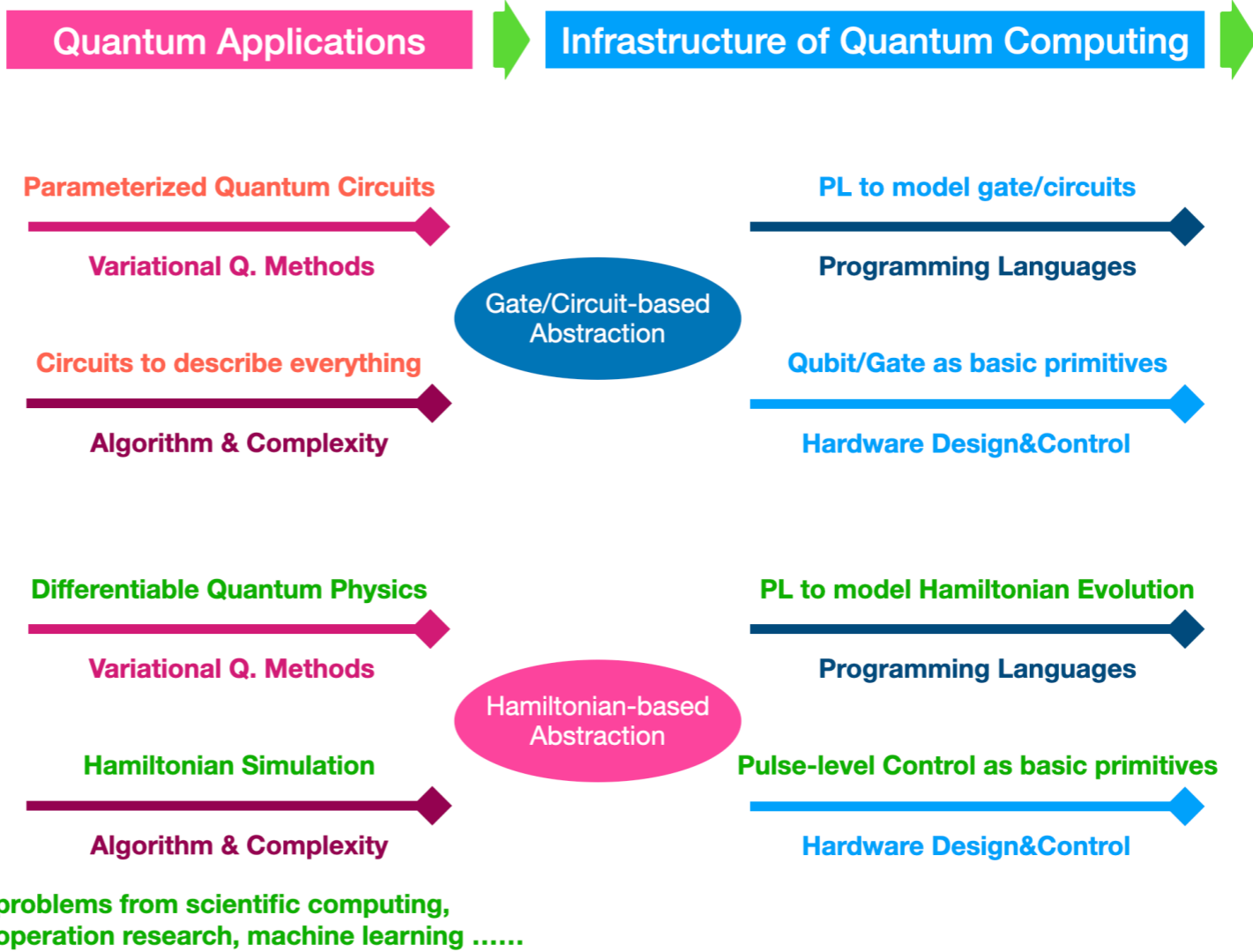
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- Xiong Fan (2020-2021. Assistant Prof. at Rutgers)
- Robert Rand (2018-2020. Assistant Prof. at U Chicago)



Thank You!

