



# Uncertainty in Computation: Artificial Intelligence and Machine Learning

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# Representing and Reasoning under uncertainty

- An agent may be uncertain about
  - the state of the world or the results of its actions due to
    - Partial observability
    - Non-determinism
  - its knowledge of the world

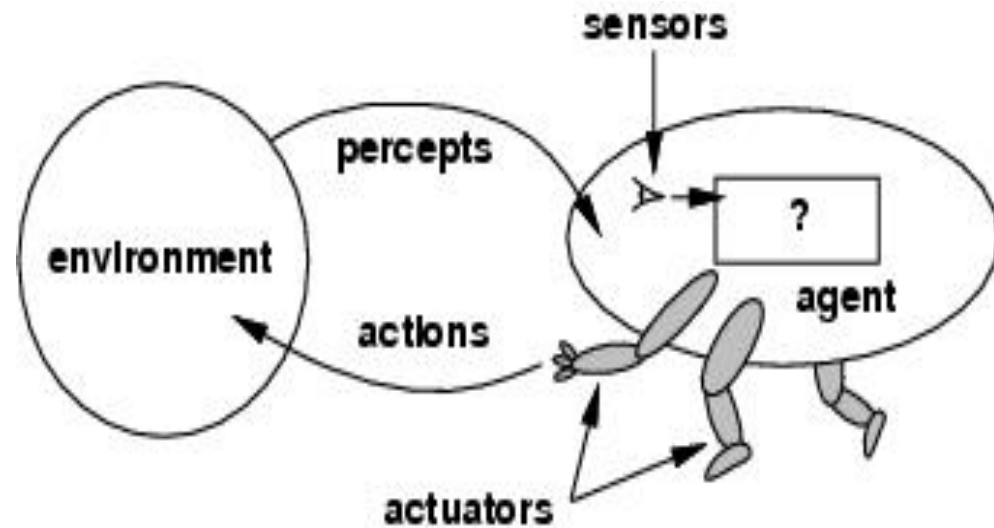


Figure source: Russell and Norvig

# Uncertainty measures

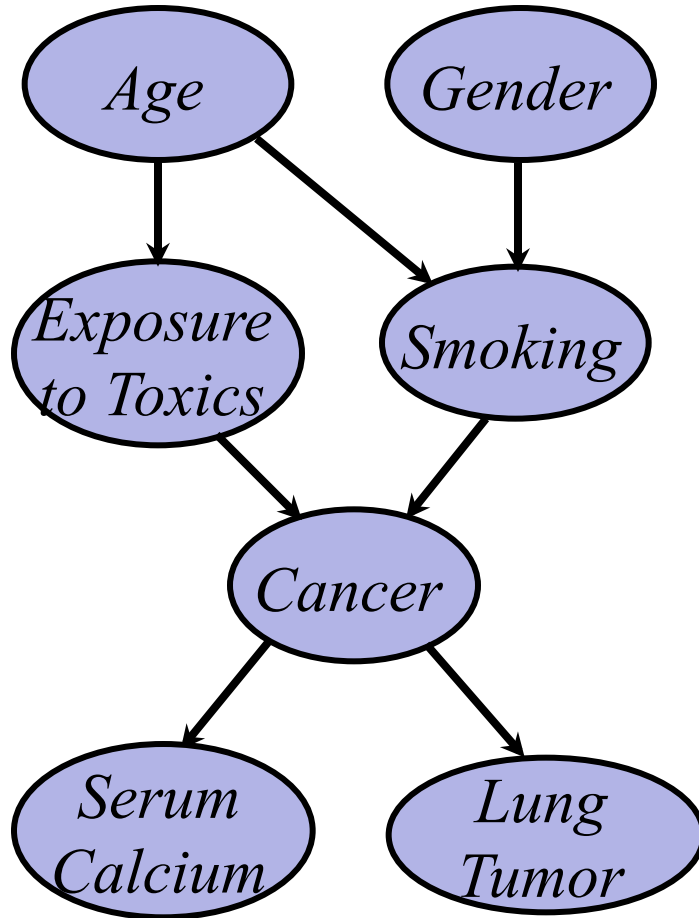
- **Probability measure**
- Imprecise probabilities – useful in settings where probabilities are only partially specified, e.g., in terms of upper and lower bounds [Walley, 1991; Kuznetsov, 1991]
- Dempster-Shafer belief functions [Dempster 1967; Shafer, 1976]
- Possibility measures [Zadeh, 1978; Dubois and Prade, 1978]
- Ranking functions [Levi, 1985]
- Plausibility measures – generalization of all of the above [Halpern, 2005]

# Probability Theory as a Knowledge Representation

- **Ontological commitments** (what can we talk about?)
  - Sentences that represent an agent's beliefs about the world
- **Epistemological Commitments** (what can we know)
  - The *probability* that a given sentence is true
- **Syntax**
  - Propositional logic based
- **Semantics**
  - Possible worlds interpretation
- **Proof Theory**
  - Based on logic and probability

$$P(\varphi) = \sum_{\omega|\varphi} \mu(\omega)$$

# Propositional probability models – Bayes Networks



Pearl, J. Probabilistic reasoning in intelligent systems. Cambridge Univ. Press. 1998.

- Nodes denote random variables
- DAG encodes a set of conditional independence relationships between random variables
- Each variable is conditionally independent of its non-descendants given its parents

$$P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | Parents(X_i))$$

- Factorized representation admits efficient inference

$$P(A, G, E, S, C, L, SC) = P(A)P(G)P(E | A)P(S | A, G)P(C | E, S)P(SC | C)P(L | C)$$

# First order probability models

- Can we combine probability with the expressive power of first order logic (FOL) representation?
- Problem: The set of possible worlds represented by an FOL sentence can be infinite
- Relational probability models (RPM) ‘solve’ this problem by replacing standard FOL semantics by database semantics
  - Unique names assumption (e.g., each customer has a unique ID)
  - Domain closure assumption (there are no more objects beyond the ones that have been named)

Koller, Pfeffer, Getoor et al. 1999-2007

# Open universe probability models

- Unique names assumption and domain closure assumption do not hold in the presence of uncertainty about existence and identity of objects
- Open universe probability models (OUPMs) extend Bayes networks and RPMs by adding
  - generative steps that add objects to the possible world under construction
  - where the number and type of objects added may depend on the objects that are already present

Milch et al., 2007

# Probabilistic Programming Languages

- Logic based
  - PRISM, Problog – logic programming + probability distributions over facts [Sato and Kameya, 2001; De Raedt, Kimmig, and Toivonen, 2007]
  - BLOG – a language based on open universe probability models [Milch et al., 2007]
- Functional programming based
  - Church, Venture – extend Scheme with probabilistic semantics for specifying recursively defined generative processes [Goodman, Mansinghka, Roy, Bonawitz and Tenenbaum, 2008]
  - IBAL – a stochastic functional programming language [Pfeffer, 2007]
- Object-oriented
  - Figaro – an expressive language with support for directed and undirected probabilistic graphical models, OUPMs, models defined over complex data structures. [Pfeffer, 2009]



# Causal Bayesian Networks

- A **causal BN** is a BN with an explicit requirement that the relationships be causal [Pearl, 2000]
- If an intervention on node  $X$  (an action written as  $do(X=x)$ ) sets  $X=x$  then the distribution changes to that obtained by cutting the links from  $Parents(X)$  to  $X$ , and setting  $X$  to  $x$ 
  - Identifiability – determining whether a given set of causal assumptions is sufficient for determining causal effects from observations and experiments [Tian and Pearl, 2002; Huang, 2006; Shpitser and Pearl, 2006 ..]
  - z-Identifiability – estimating the effect of intervening on a set of variables  $X$  from experiments on a different set,  $Z$  [Bareinboim and Pearl, 2012]
  - Transportability – reuse of causal information obtained from experiments in one setting in a related but different setting where only observations are available [Bareinboim and Pearl, 2012; Lee and Honavar, 2013; Bareinboim and Pearl 2013]
  - Generalizations of the above [Bareinboim, Lee, Honavar, Pearl, 2013]

# Uncertainty in machine learning

- Data uncertainty
  - missing attribute values, partially specified attribute values
  - missing class labels, partially specified class labels
  - distributional data
- Need to generalize standard algorithms that cope with data uncertainty
  - Partially specified instances [Zhang et al, 2003; 2006]
  - Partially specified class labels e.g., “multiple instance learning”, “semi-supervised learning”, “structured label learning” ...
  - Distributional data [Lin et al., 2013; Muandet et al., 2012]

# Uncertainty in machine learning

- Model uncertainty
  - Is the assumed hypothesis class appropriate? (a form of epistemic uncertainty)
  - Can we trust the model parameters (pre-specified? learned?)
  - Can we trust the reported performance?
  - How can we update uncertainty?
  - How can we propagate uncertainty?