

Molecular Mechanical Computing

Institute for Molecular Manufacturing

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Mechanical Computing Systems Using Only Links and Rotary Joints

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Journal of Mechanisms and Robotics, Dec 2018, 10(6): 061006

<https://doi.org/10.1115/1.4041209>

Evaluating the friction of rotary joints in molecular machines

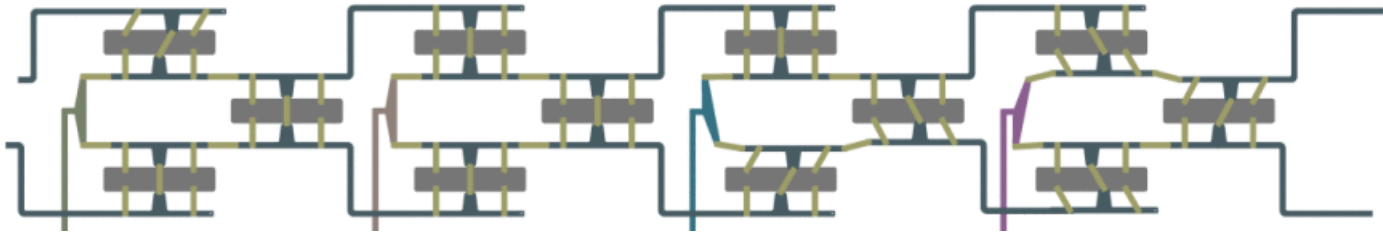
Tad Hogg, Matthew S. Moses and Damian G. Allis

Molecular Systems Design & Engineering, 2017, 2, 235-252

<https://doi.org/10.1039/C7ME00021A>

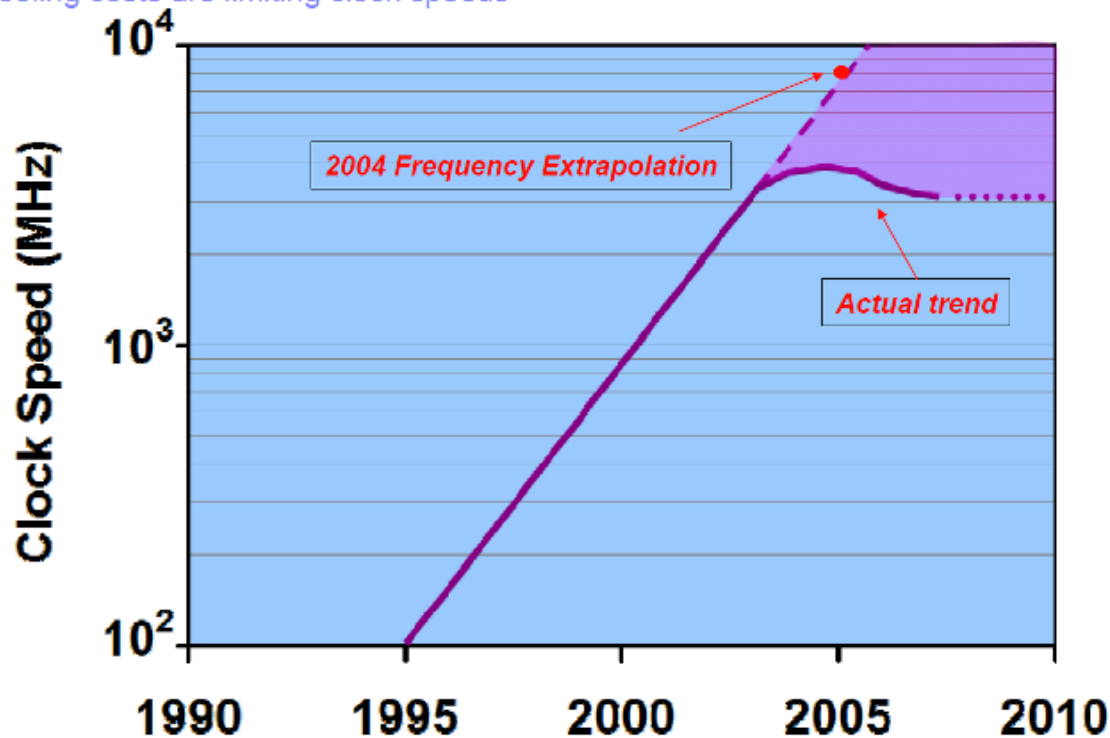
Conclusion:
 10^{21} FLOPS
In a sugar cube
Using 1 watt of power
With a 100 MHz clock (10 ns)

Key concept: 4-phase two rail mechanical reversible shift register

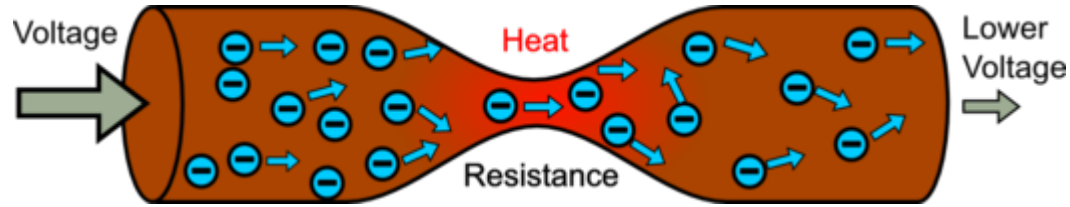


Microprocessor Clock Speeds

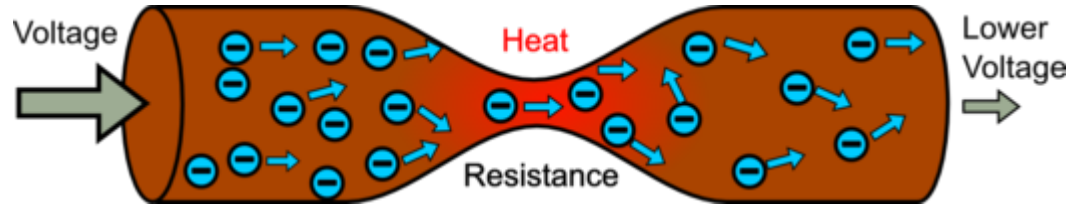
Cooling costs are limiting clock speeds



The Problem: I^2R

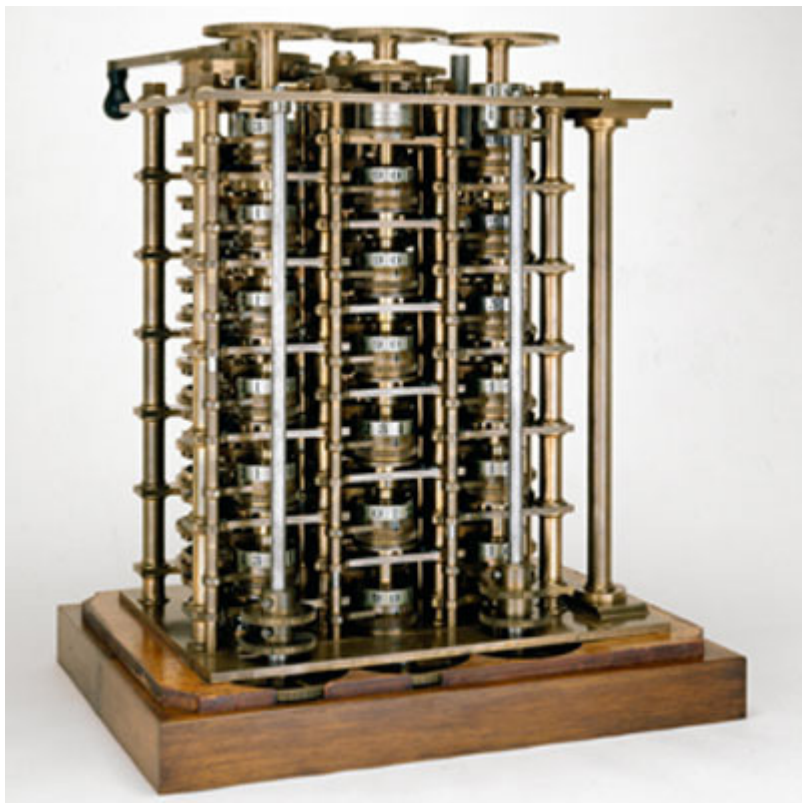


Typical nanoscale contacts are $\sim 13\text{k}\Omega^*$
One electron moving 10 nm in 10 ns dissipates
 $\sim 3 \times 10^{-18}$ J or ~ 750 times kT



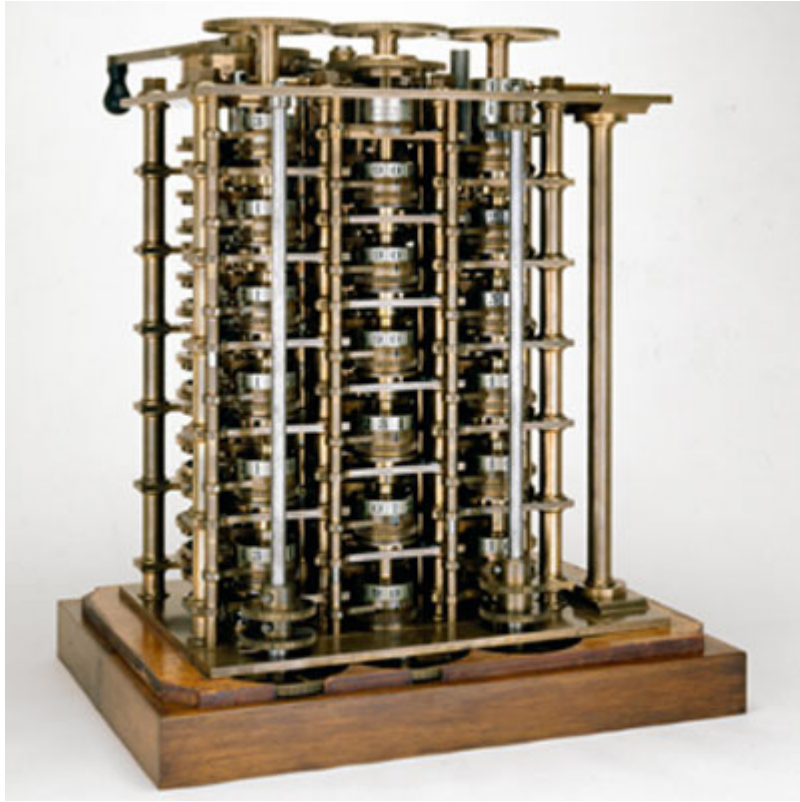
*See the Landauer Formula, https://en.wikipedia.org/wiki/Landauer_formula. Although resistive losses can be avoided by adiabatic switching this raises other issues; see, for example, Helical Logic (<http://www.zyvex.com/nanotech/helicalIntro.html>).

Are there alternatives to electronics?



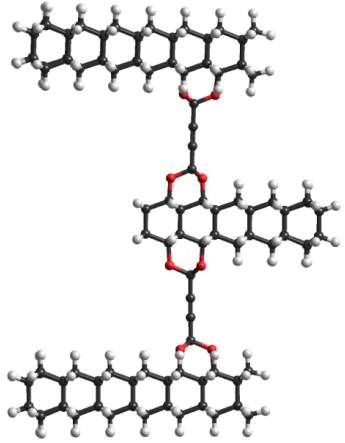
Mechanical Computing

www.imm.org/Reports/rep046.pdf



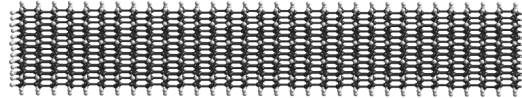
But!

Snapping, sliding, dragging,
squeezing, forcing,
pounding, smashing,
ringing, tensioning, etc. etc.
etc.



**Rotary
Joints**

+



**Links
(10 to 20 nm)**

+

Clocks

**Periodic
1 Piconewton
Forces**

System Rules

- The periodic clocking forces are ~ 1 piconewton.
- Links make contact only through rotary joints.
- There are no unconstrained degrees of freedom.
- The system is driven by a four-phase clock.
- The system is fully reversible.

Additional Perspectives

- The time, t , uniquely determines the position of every link in the system, up to the uncertainty caused by thermal noise.
- The system can operate as slowly as might be desired.
- The system can operate both forwards and in reverse.

**How do we compute
under these constraints?**

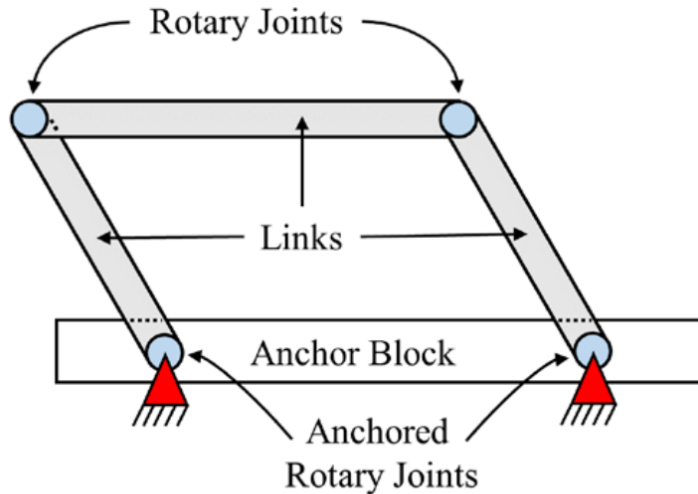
We will define two primitives:

- 1) A lock

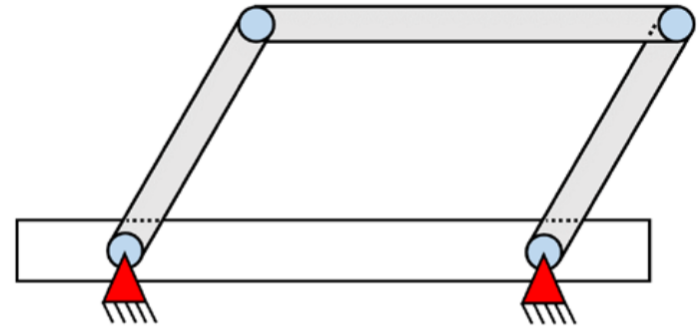
- 2) A balance

We will then use these two primitives, along with the periodic clocking forces, to implement a shift register.

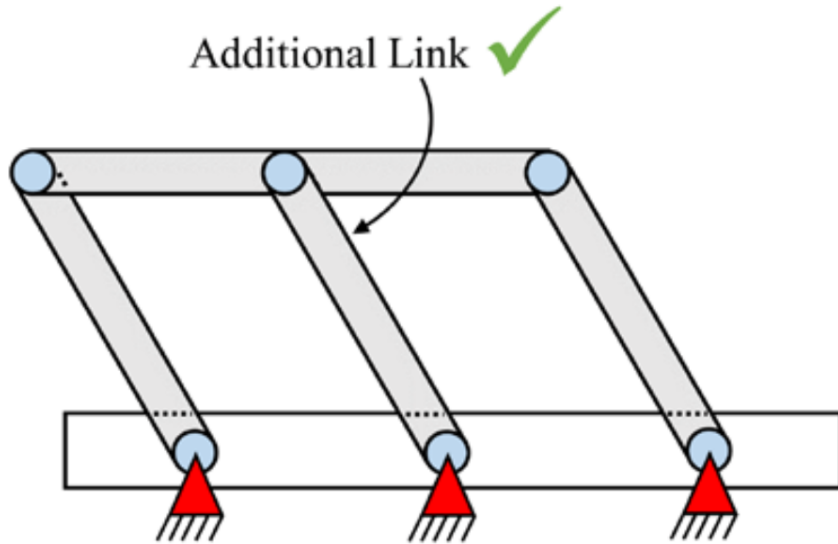
A data link can be in one of two positions.
One of these positions is 0, the other is 1.



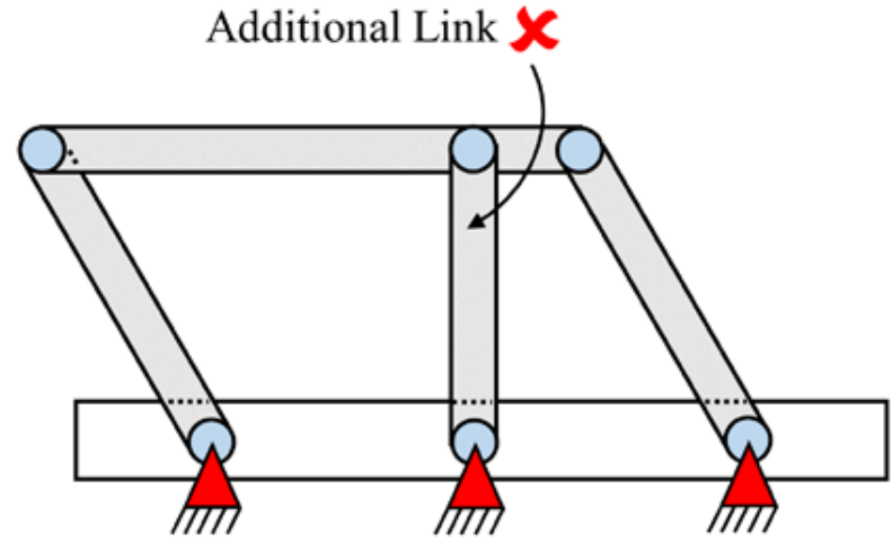
4-Bar Linkage, Left-leaning



4-Bar Linkage, Right-leaning

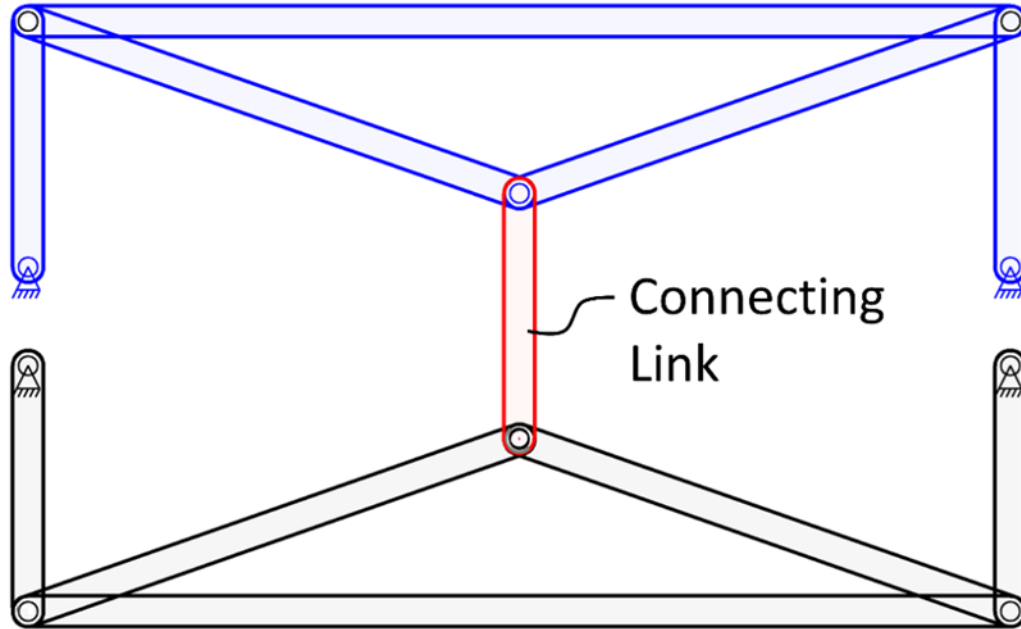


Mobile linkage



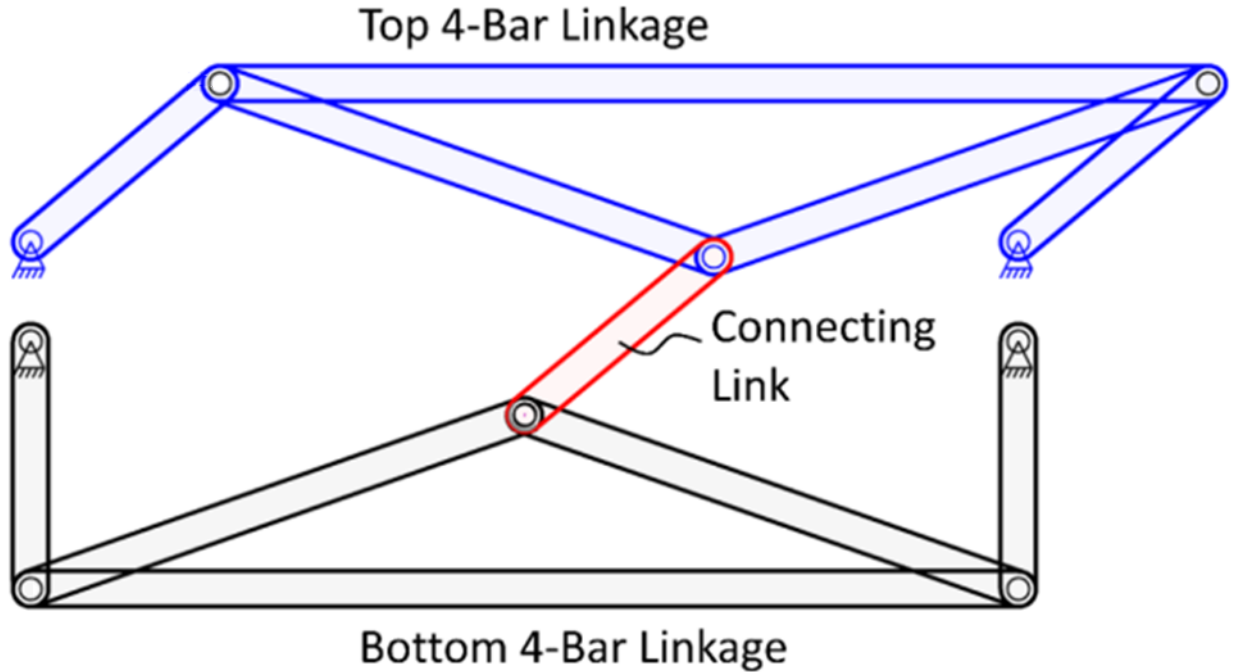
Non-mobile linkage

Top 4-Bar Linkage

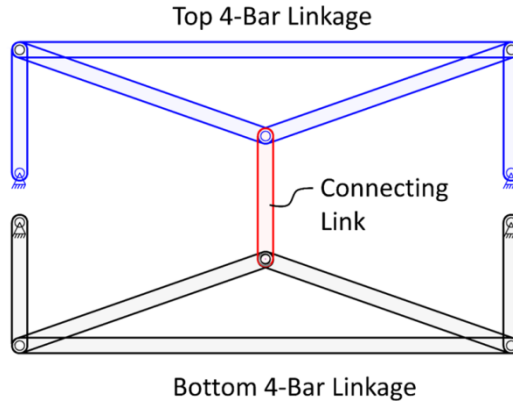


Bottom 4-Bar Linkage

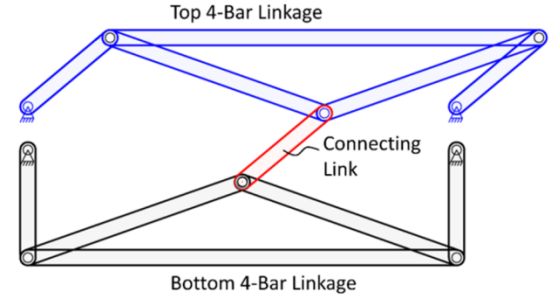
A lock in the (0,0) position



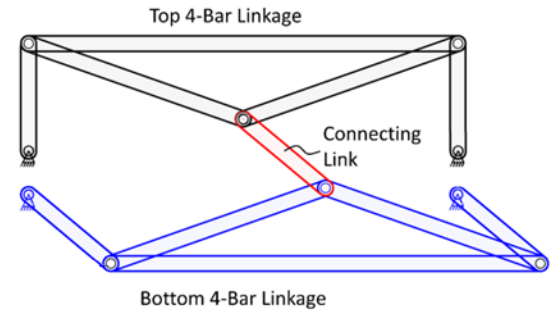
A lock in the (1,0) position



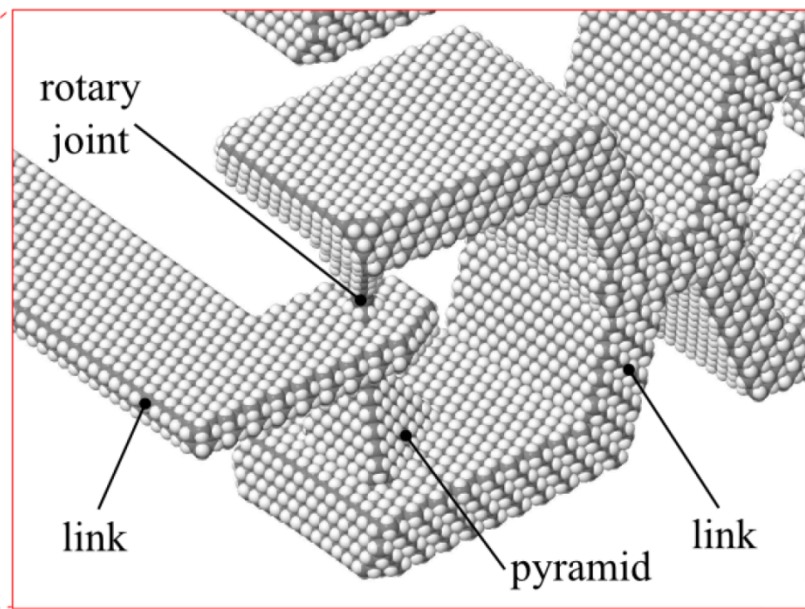
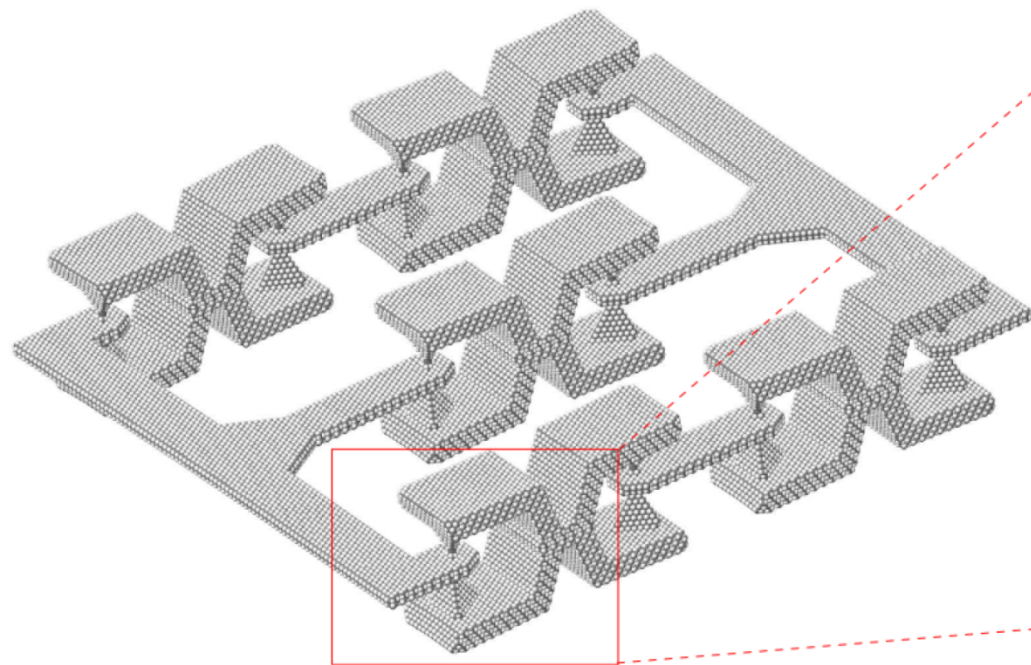
A lock in the (0,0) position



A lock in the (1,0) position



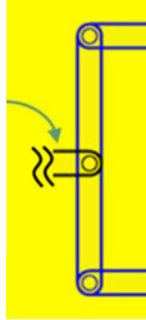
A lock in the (0,1) position



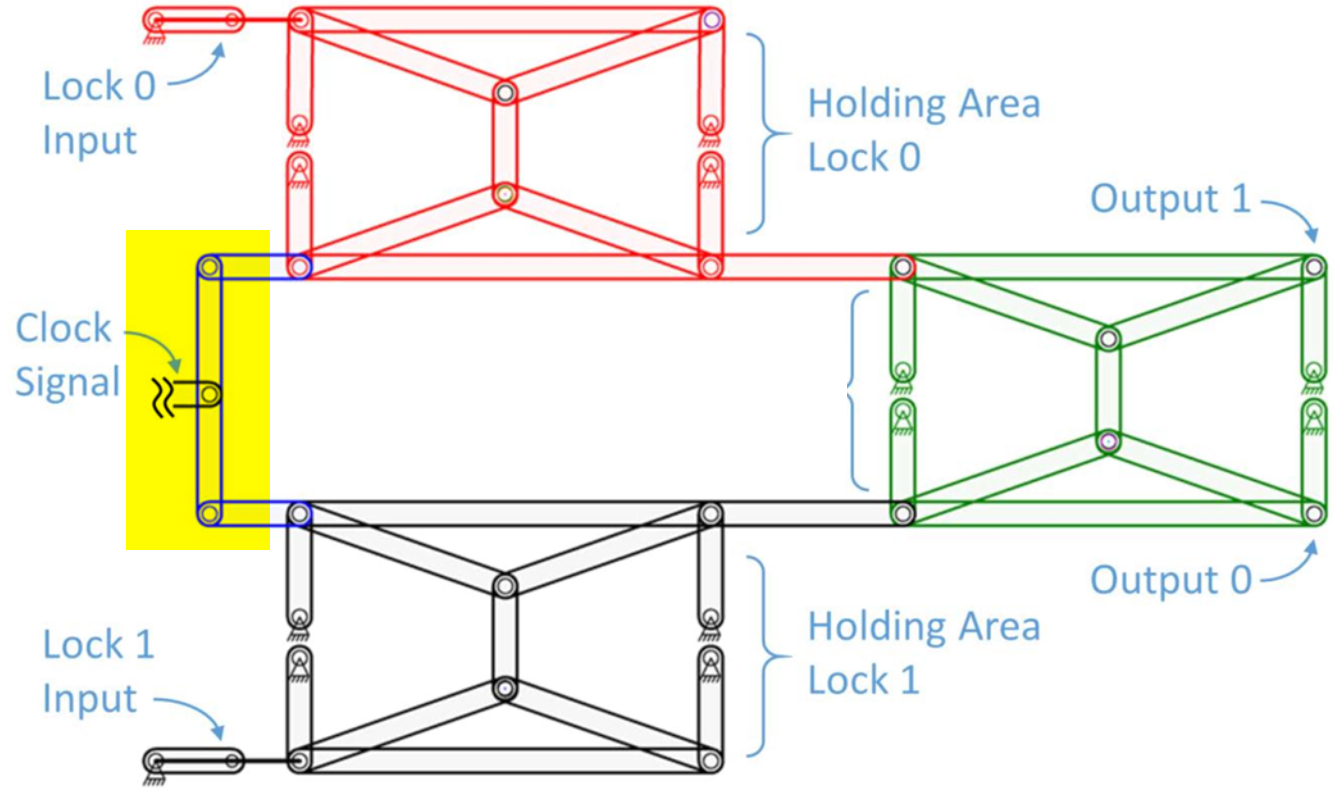


Balance

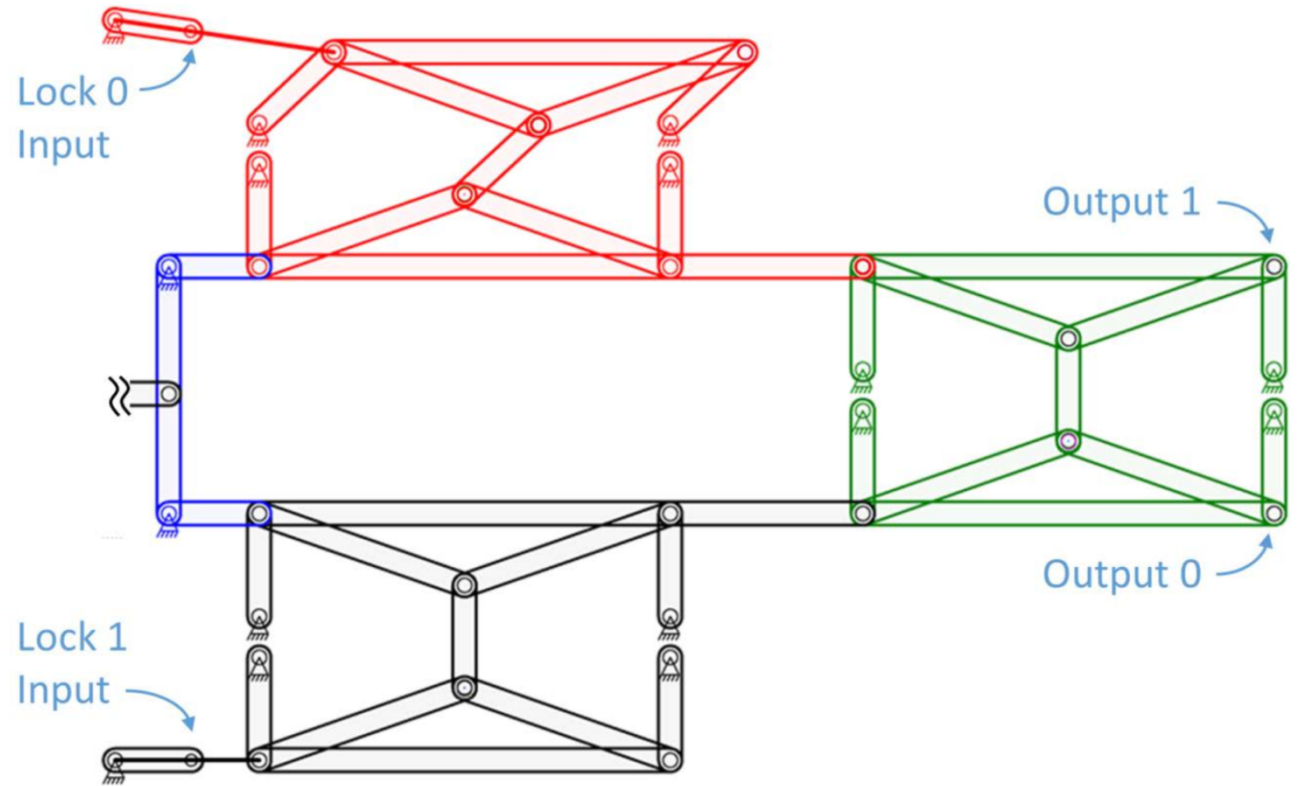
A balance



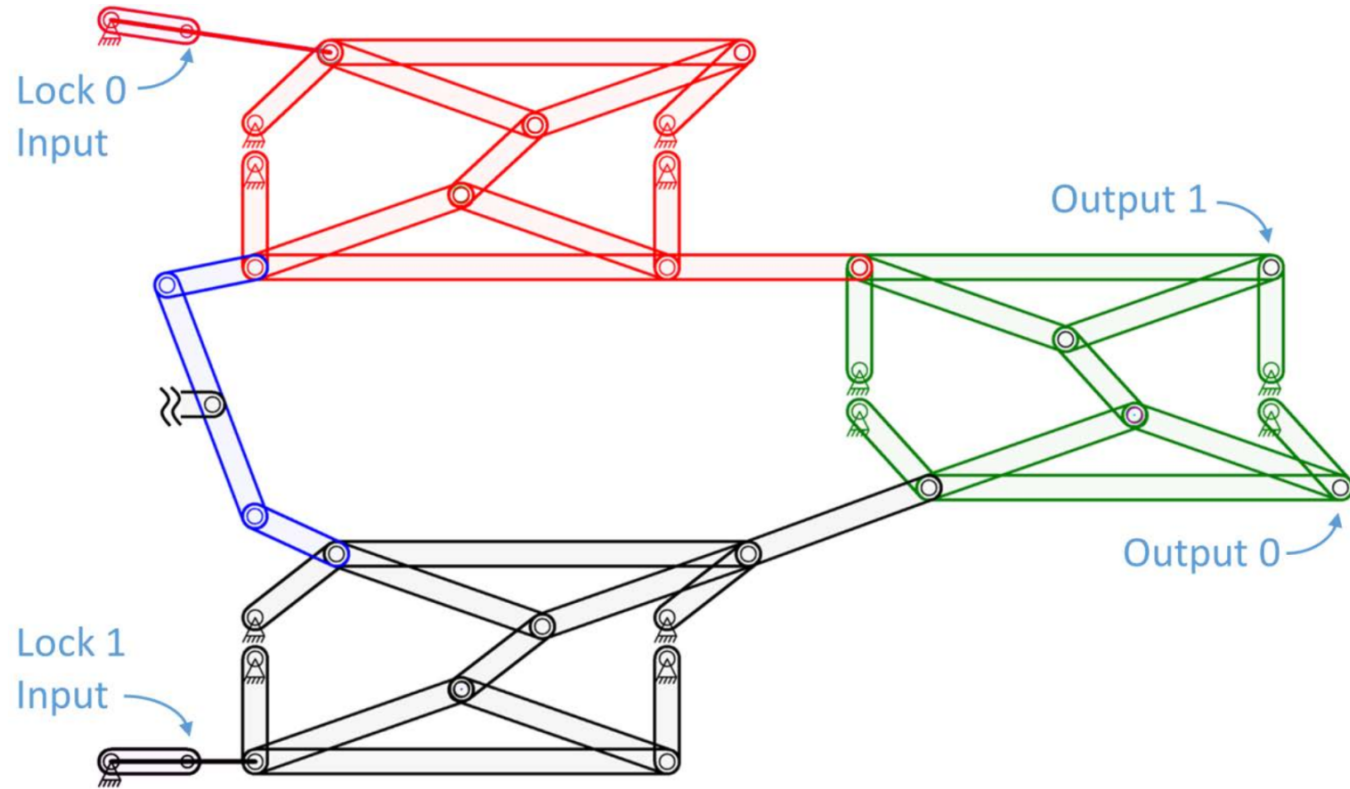
A balance
connected
to two locks



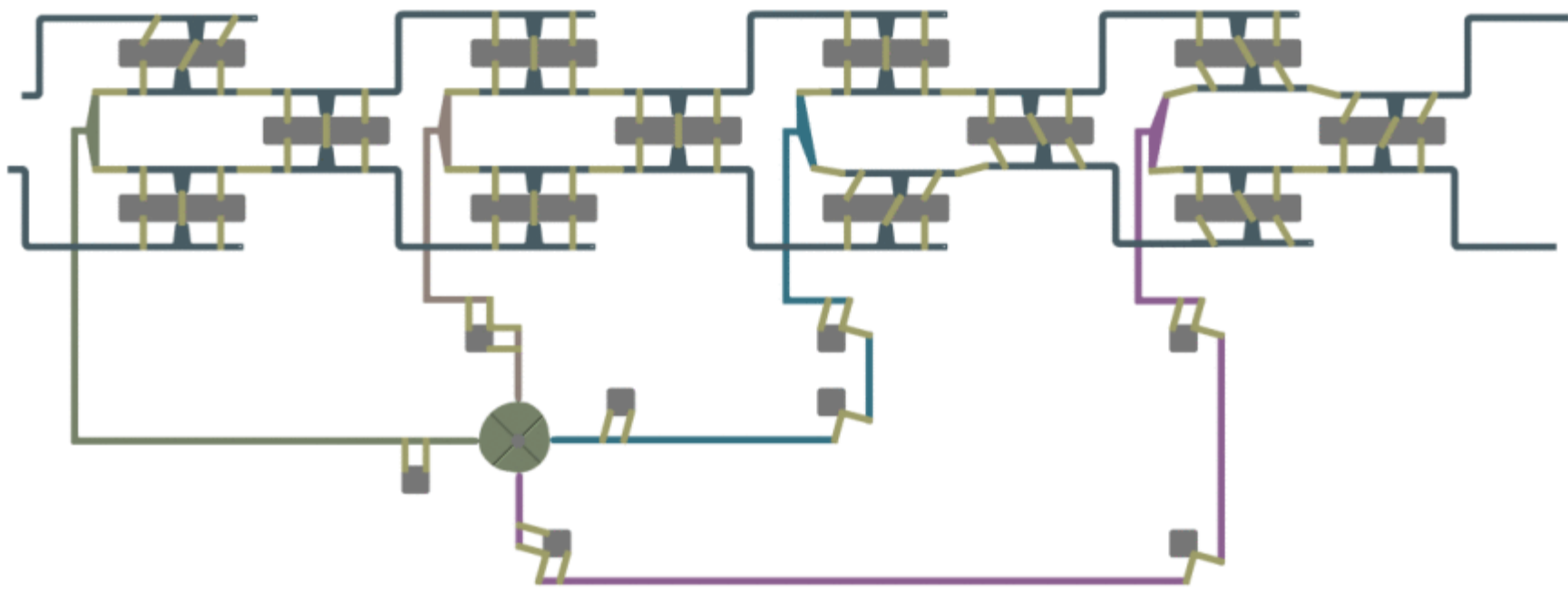
Shift register cell in the (0,0) blank state



Shift register cell with input (1,0), prior to clock actuation

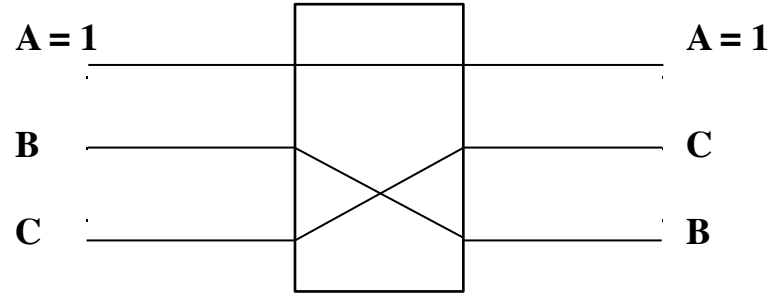
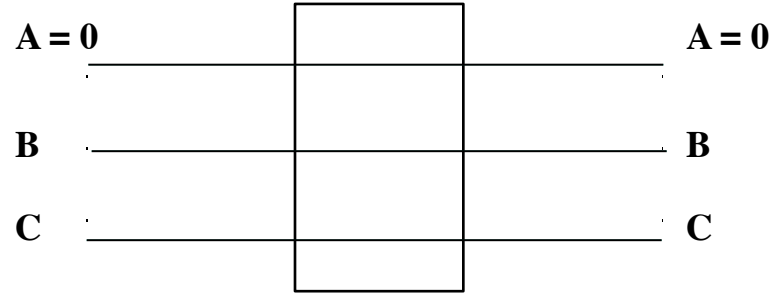


Shift register cell with input (1,0) after clock actuation



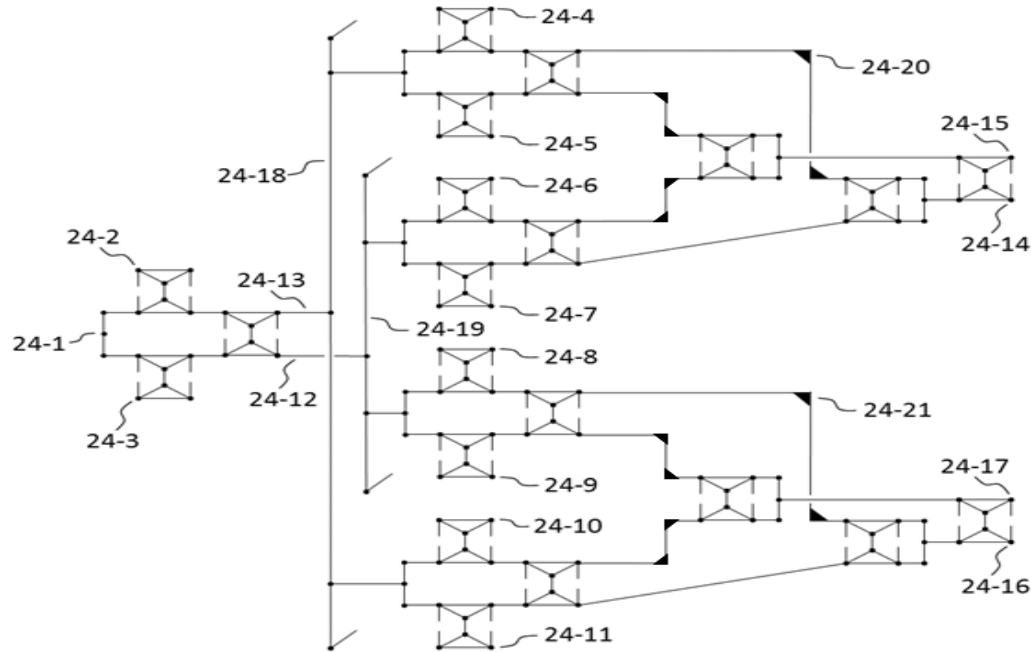
Fredkin Gate

(logically complete)



Mechanical Clocked Fredkin Gate

(from December 2015 patent filing*)



*Mechanical Computing Systems,
<http://www.merkle.com/papers/MechanicalComputingSystems.pdf>

What's the energy dissipation?

- 1) Rotary joints have very little drag**
- 2) Other dissipative mechanisms can have less drag**

Rotary Drag Power Equation

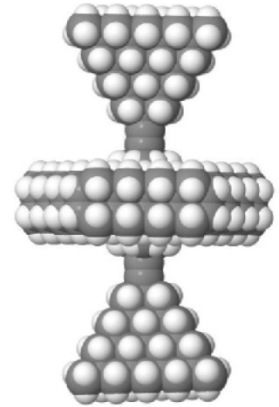
$$P_{rd} = K_{rd} \nu_r^2$$

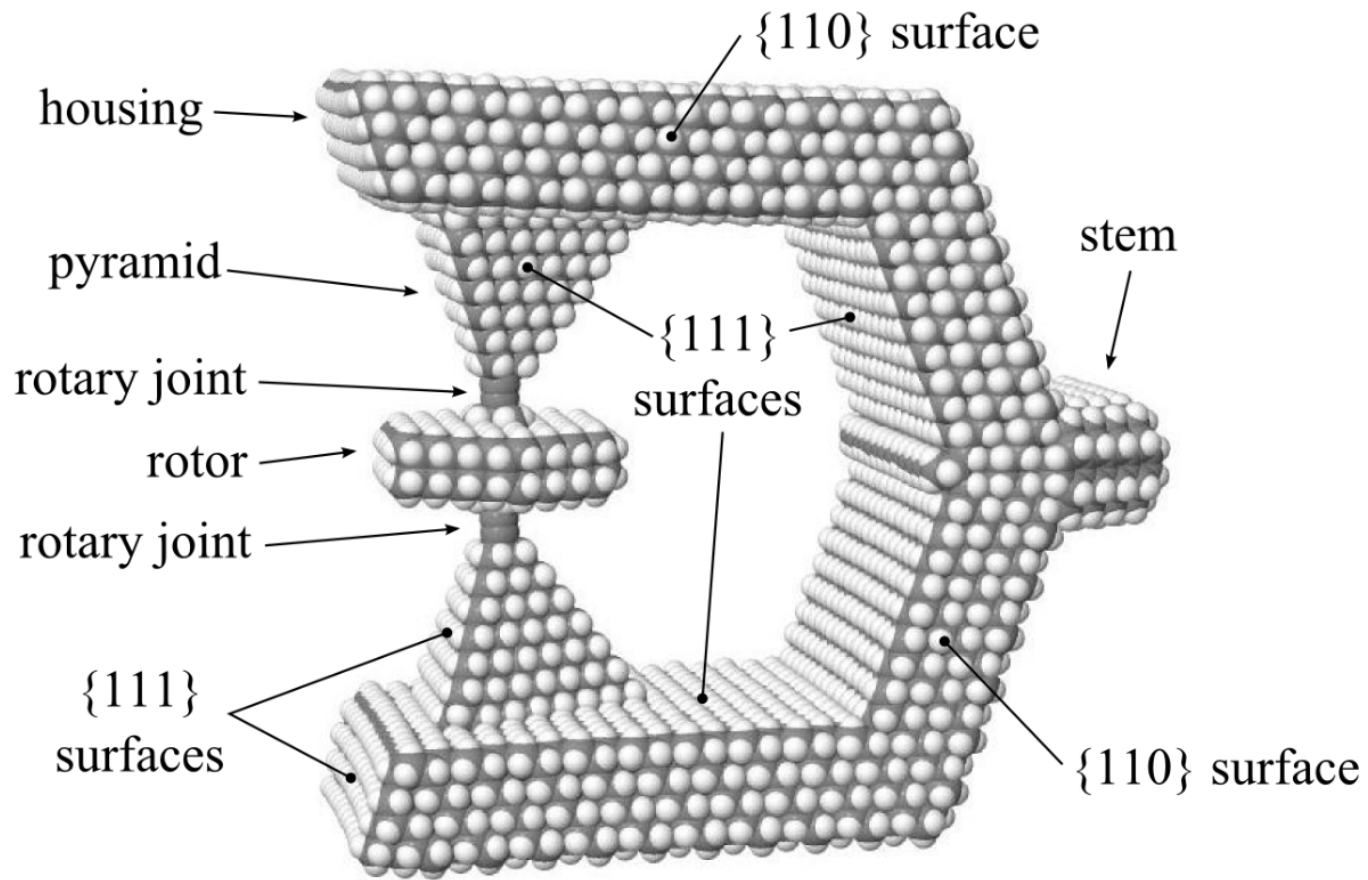
where:

P_{rd} is the power dissipated (in watts) by rotary drag

K_{rd} is the applicable rotary drag coefficient
(in J·s or kg m²/s)

ν_r is the rotational speed (in radians/second)
between the housing and the rotor





$$K_{rd} \sim 2 \times 10^{-35} \text{ J s}$$

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What's the energy dissipation?

- 1) Count the rotary joints
- 2) Determine their rotational speed
- 3) Apply the equation $P_{rd} = K_{rd} v_r^2$
- 4) Neglect other dissipative mechanisms

Dissipative Mechanisms Considered

Sliding drag (none)

“Snap to” (none)

EM radiation (none)

Resistive losses (none)

Resonance mechanisms (very small)

Acoustic radiation (very small)

Acoustic radiation (extremely small when canceled)

Entropic losses (extremely small)

Heat flows caused by stress/strain (extremely small)

Thermal equilibration times (under 1 ps)

10^{21} FLOPS* per watt in a Sugar Cube

- More efficient gate implementations
- More efficient implementations of floating point operations
- 10^{21} FLOPS per watt seems achievable

*Floating Point Operations Per Second (<https://en.wikipedia.org/wiki/FLOPS>)

END OF TALK